

	INDIAN SCHOOL AL WADI AL KABIR	
Class: XI	Department: SCIENCE 2024 – 25 SUBJECT: PHYSICS	Date of submission: 03-02-2025
Worksheet No: 12 WITH ANSWERS	CHAPTER / UNIT: KINETIC THEORY	Note: A4 FILE FORMAT
NAME OF THE STUDENT:	CLASS & SEC:	ROLL NO.:

OBJECTIVE TYPE QUESTIONS

- In the equation, $PV = RT$, the V refers to the volume of:
 - 1 g of a gas
 - 1 mole of a gas
 - 1 kg of gas
 - any amount of gas
- A gas behaves as an ideal gas at
 - low pressure and high temperature
 - low pressure and low temperature
 - high pressure and low temperature
 - high pressure and high temperature
- Gases deviate from perfect gas behaviour because their molecules
 - are polyatomic
 - are of very small size
 - don't attract each other
 - interact with each other through intermolecular forces
- The translational kinetic energy of gas molecules for 1 mol of gas is equal to
 - $\frac{3}{2} RT$
 - $\frac{2}{3} KT$
 - $\frac{RT}{2}$
 - $\frac{3}{2} KT$
- The work done by (or on) a gas per mole per kelvin is called
 - Universal gas constant
 - Boltzmann's constant
 - Gravitational constant
 - Entropy
- Dimensional formula for universal gas constant R is given by
 - $[ML^2T^{-2}K^{-1}]$
 - $[ML^2T^{-3}K^{-1}]$
 - $[M^{\circ}L^2T^{-3}K^{-1}]$
 - $[ML^2T^{-2}K^{-1}]$
- An ant is walking on the horizontal surface. The number of degrees of freedom of ant will be
 - 1
 - 2
 - 3
 - 6
- The specific heat of a gas
 - has only two values C_p & C_v
 - has a unique value of given temperature
 - can have any values from 0 to ∞
 - depends upon the mass of the gas

9. Who gave the law of equipartition of energy?

- (a) Maxwell (b) Clausius
(c) Boltzmann (d) Carnot

ASSERTION - REASON BASED QUESTIONS

Direction: - In the following questions, a statement of assertion is followed by a statement of reason. Mark the correct choice as:

- (a) If both assertion and reason are true and reason is the correct explanation of assertion.
(b) If both assertion and reason are true but reason is not correct explanation of assertion.
(c) If assertion is true, but reason is false.
(d) If both assertion and reason are false.

10. Assertion: If a gas container in motion is suddenly stopped, the temperature of the gas rises.
Reason: The kinetic energy of ordered mechanical motion is converted into the kinetic energy of random motion of gas molecules.

11. Assertion: The total translational kinetic energy of all the molecules of a given mass of an ideal gas is 1.5 times the product of its pressure and its volume.
Reason: The molecules of a gas collide with each other and the velocities of the molecules change due to collision.

12. Assertion: Gases do not settle to the bottom of a container.
Reason: Gases have high kinetic energy.

13. Assertion: A gas can be liquified at any temperature by increase of pressure alone.
Reason: On increasing pressure the temperature of gas decreases.

14. Assertion: Equal masses of helium and oxygen gases are given equal quantities of heat. There will be a greater rise in the temperature of helium compared to that of oxygen.
Reason: The molecular weight of oxygen is more than the molecular weight of helium.

CASE STUDY BASED QUESTIONS: -

15. The equipartition of kinetic energy was proposed initially in 1843 and more correctly in 1845, by John James Waterston. In 1859, James Clerk Maxwell argued that the kinetic heat energy of a gas is equally divided between linear and rotational energy. In 1876, Ludwig Boltzmann expanded on this principle by showing that the average energy was divided equally among all the independent components of motion in a system. Boltzmann applied the equipartition theorem to provide a theoretical explanation of the Dulong-Petit law for the specific heat capacities of solids.

Law of Equipartition of Energy

According to this law, for any system in thermal equilibrium, the total energy is equally distributed among its various degree of freedom. And each degree of freedom is associated with energy $\frac{1}{2} kT$ (where

$k = 1.3 \times 10^{-23} \text{ J/K}$, T = absolute temperature of the system).

At a given temperature T ; all ideal gas molecules no matter what their mass have the same average translational kinetic energy; namely, $\frac{3}{2} kT$. When we measure the temperature of a gas, we are also measuring the average translational kinetic energy of its molecules. At same temperature gases with different degrees of freedom (e.g., He and H) will have different average energy or internal energy namely $\frac{f}{2} kT$. (f is different for different gases)

Answer the following questions

i. Relation between pressure P and average kinetic energy E per unit volume of a gas is

- (a) $P = \frac{2E}{3}$ (b) $P = \frac{E}{3}$ (c) $P = \frac{3E}{2}$ (d) $P = 3E$

- ii. At 0 K, which of the following properties of a gas will be zero?
 (a) kinetic energy (b) potential energy
 (c) vibrational energy (d) density
- iii. An ant is walking on the horizontal surface. The number of degrees of freedom of ant will be
 (a) 1 (b) 2 (c) 3 (d) 6
 Or
- iv. The number of degrees of freedom for a diatomic gas molecule is
 (a) 2 (b) 3 (c) 5 (d) 6

SHORT ANSWER TYPE QUESTIONS

16. For ideal behavior of a gas, state the condition in terms of density of the gas.
17. A container filled with Helium gas at 300 K is heated to 600K. The coefficient of thermal expansion of the container is negligible. Calculate the change in the average K.E. of the helium atoms.
18. When a scooter runs for a long time, the air pressure in its tyres increases slightly.
19. On what factors does the average kinetic energy of gas molecules depend : Nature of the gas, temperature, volume?
20. Obtain the dimensional formula for R used in the ideal gas equation $PV = RT$.

LONG ANSWER TYPE QUESTIONS

21. . An air bubble of volume 1.0 cm³ rises from the bottom of a lake 40 m deep at a temperature of 12°C. To what volume does it grow when it reaches the surface which is at a temperature of 35°C?
22. A vessel is filled with a gas at a pressure of 76 cm of mercury at a certain temperature. The mass of the gas is increased by 50% by introducing more gas in the vessel at the same temperature. Find out the resultant pressure of the gas.
23. An oxygen cylinder of volume 30 liter has an initial gauge pressure of 15 atmosphere and a temperature of 27°C. After some oxygen is withdrawn from the cylinder, the gauge pressure drops to 11 atmosphere and its temperature drop to 17°C. Estimate the mass of oxygen taken out of the cylinder.
 $(R = 8.31/\text{mol}^{-1} \text{K}^{-1})$ (molecular mass of O₂ = 32)
24. At what temperature the rms speed of oxygen atom equal to r.m.s. speed of helium gas atom at - 10°C?, Atomic mass of helium = 4, Atomic mass of oxygen = 32.
25. Estimate the total number of molecules inclusive of oxygen, nitrogen, water vapour and other constituents in a room of capacity 25.0 m³ at a temperature of 27°C and 1 atmospheric pressure.

ANSWER KEY	
1	(b) 1 mole of a gas
2	(a) low pressure and high temperature
3	(d) interact with each other through intermolecular forces
4	(a) $3/2RT$
5	(a) Universal gas constant
6	(a) $[ML^2T^{-2}K^{-1}]$
7	(b) 2
8	(c) can have any values from 0 to ∞
9	(a) Maxwell
10	(a) If both assertion and reason are true and reason is the correct explanation of assertion.

11	(b) If both assertion and reason are true but reason is not correct explanation of assertion.
12	(a) If both assertion and reason are true and reason is the correct explanation of assertion.
13	(d) If both assertion and reason are false.
14	(b) If both assertion and reason are true but reason is not correct explanation of assertion
15	$(a) P = \frac{2E}{3}$ i. ii. (a) kinetic energy iii. (b) 2 iv. (c) 5
16	For ideal gas, $P = \rho RT$ For ideal behavior, ρ should be low.
17	$\text{Average K.E.} = \frac{3}{2} kT$ $\therefore \text{Change in average K.E.}$ $= \frac{3}{2} k(600 - 300) = \frac{3}{2} \times 300 \times 1.38 \times 10^{-23} \text{ Joule} = 6.21$ $\times 10^{-21} \text{ Joule}$
18	On running the scooter, the work done against friction is converted to heat. $P \propto T$, so, as the temperature of the tyre increases, pressure will also increase.
19	The average kinetic energy of the molecules of a gas depends only on temperature
20	$\text{Since } PV = RT$ $\text{So } R = \frac{PV}{T} = \frac{FV}{AT} \quad \text{or} \quad R = \frac{[MLT^{-2}][L^3]}{[L^2][K]}$ $\text{or } R = [ML^2T^{-2}K^{-1}]$
21	$V_1 = 10^{-6} \text{ m}^3$ Pressure on bubble $P_1 = \text{Water pressure} + \text{Atmospheric pressure}$ $= pgh + P_{\text{atm}}$ $= 4.93 \times 10^5 \text{ Pa}$ $T_1 = 285 \text{ K}, T_2 = 308 \text{ K}$ $\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$ $V_2 = \frac{4.93 \times 10^5 \times 1 \times 10^{-6} \times 308}{285 \times 1.01 \times 10^5} = 5.3 \times 10^{-6} \text{ m}^3$
22	According to kinetic theory of gases, $PV = \frac{1}{3} m v_{\text{rms}}^2$ At constant temperature, v_{rms}^2 is constant. As v is also constant, so $P \propto m$. When the mass of the gas increase by 50% pressure also increases by 50%, $\therefore \text{Final pressure} = 76 + \frac{50}{100} \times 76 = 114 \text{ cm of Hg.}$

23	$V_1 = 30 \text{ litre} = 30 \times 10^3 \text{ cm}^3 = 3 \times 10^{-2} \text{ m}^3$ $P_1 = 15 \times 1.013 \times 10^5 \text{ N/m}^2$ $T_1 = 300 \text{ K}$ $\mu_1 = \frac{P_1 V_1}{RT_1} = 18.3$ $P_2 = 11 \times 1.013 \times 10^5 \text{ N/m}^2$ $V_2 = 3 \times 10^{-2} \text{ m}^3$ $T_2 = 290 \text{ K}$ $\mu_2 = \frac{P_2 V_2}{RT_2} = 13.9$ $\mu_2 - \mu_1 = 18.3 - 13.9 = 4.4$ Mass of gas taken out of cylinder $= 4.4 \times 32 \text{ g}$ $= 140.8 \text{ g}$ $= 0.140 \text{ kg.}$
24	$v_{\text{rms}} = \left[\frac{3PV}{M} \right]^{1/2} = \left[\frac{3RT}{M} \right]^{1/2}$ Let r.m.s. speed of oxygen is $(v_{\text{rms}})_1$ and of helium is $(v_{\text{rms}})_2$ is equal at temperature T_1 and T_2 respectively. $\frac{(v_{\text{rms}})_1}{(v_{\text{rms}})_2} = \sqrt{\frac{M_2 T_1}{M_1 T_2}}$ $\left[\frac{4T_1}{32 \times 263} \right]^{1/2} = 1$ $T_1 = \frac{32 \times 263}{4} = 2104 \text{ K.}$
25	As Boltzmann's constant, $k_B = \frac{R}{N}, \therefore R = k_B N$ Now $PV = nRT = nk_B NT$ $\therefore$ The number of molecules in the room $= nN = \frac{PV}{Tk_B}$ $= \frac{1.013 \times 10^5 \times 25.0}{300 \times 1.38 \times 10^{-23}} = 6.117 \times 10^{26}.$

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